

Lesson 15.4:

Compound Events

Essential Question

How can you find the number of possible outcomes of one or more events?

A *tree diagram* can be used to list possible outcomes in an organized way.

- 1) List the possible outcomes of the first event.
- 2) Draw a branch for each possible outcome of the second event off of each possible outcome of the first event. (Continue for as many events as you have.)
- 3) List the possible outcomes of the compound event.

You randomly choose a crust and style of pizza. Find the sample space. How many different pizzas are possible?

Crust

- Thin Crust
- Stuffed Crust

Style

- Hawaiian
- Mexican
- Pepperoni
- Veggie



- Thin Hawaiian 1
- Thin Mexican 2
- Thin Pepperoni 3
- Thin Veggie 4
- Stuffed Hawaiian 5
- Stuffed Mexican 6
- Stuffed Pepperoni 7
- Stuffed Veggie 8

What is the probability of selecting a stuffed crust Hawaiian pizza?

$$\frac{1}{8} \approx 0.13$$

*Tree diagram
*Sample space

Find the sample space of all of the possible outcomes of rolling a number cube and flipping a coin.

1	∧	H	1 H
		T	1 T
2	∧	H	2 H
		T	2 T
3	∧	H	3 H
		T	3 T
4	∧	H	4 H
		T	4 T
5	∧	H	5 H
		T	5 T
6	∧	H	6 H
		T	6 T

Key Idea

Fundamental Counting Principle

An event M has m possible outcomes. An event N has n possible outcomes. The total number of outcomes of event M followed by event N is $m \times n$.

Alternate definition: When you have a compound event, you multiply the **# of possible outcomes for event 1** by the **# of possible outcomes for event 2**.

How many different outfits can you make from the T-shirts, jeans, and shoes in the closet?

$$4 \times 7 \times 3$$

$$\downarrow$$

$$12 \times 7$$

84 outfits



2. Find the total number of possible outcomes of spinning the spinner and choosing a number from 1 to 5.

$$4 \cdot 5 = 20$$



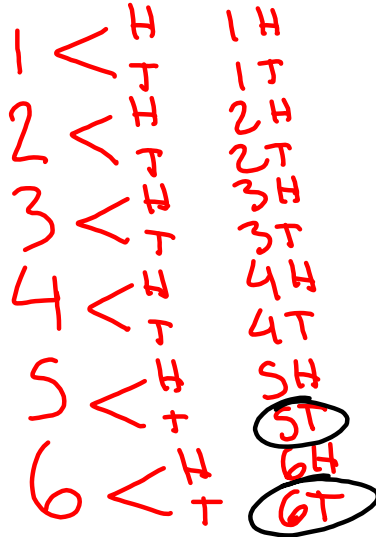
3. How many different outfits can you make from 4 T-shirts, 5 pairs of jeans, and 5 pairs of shoes?

$$4 \cdot 5 \cdot 5 = 100$$

What is the probability of rolling a number greater than 4 and flipping tails?

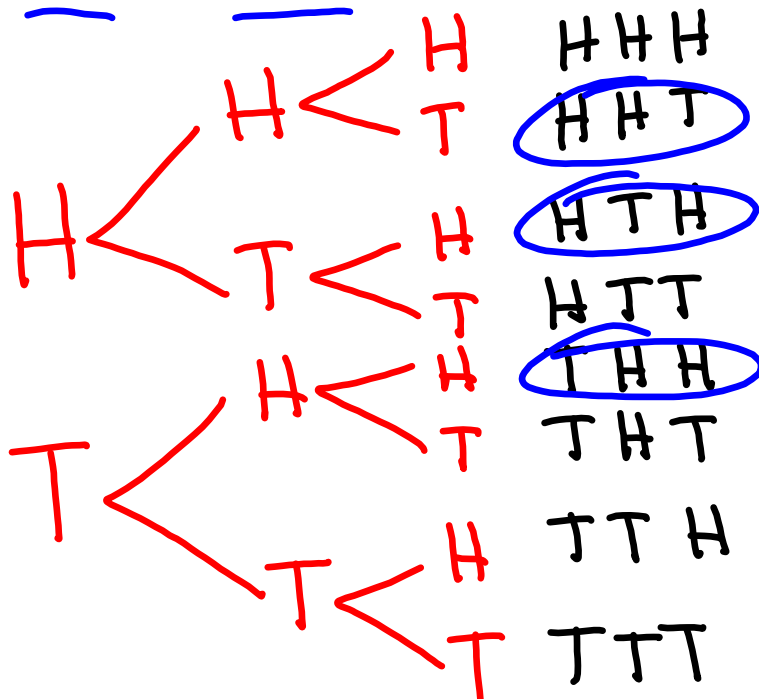
$$P(>4) \cdot P(\text{tails})$$

$$\frac{2}{6} \cdot \frac{1}{2} = \frac{1}{6} \approx 0.17$$



$$\frac{2}{12} = \frac{1}{6}$$

You flip three nickels. What is the probability of flipping two heads and one tails?



$$\frac{3}{8} \approx 0.38$$

4. What is the probability of rolling at most 4 and flipping heads?

$$\frac{2}{36} \cdot \frac{1}{2} = \frac{1}{36} \text{ or } 0.\overline{3}$$

5. What is the probability of flipping at least two tails (with 3 nickels)?

$$\begin{array}{cc} \text{TTT} & \text{HTT} \\ \text{THT} & \text{TTT} \end{array} \quad \frac{4}{8} = \frac{1}{2} \text{ or } 0.5$$

6. You roll two number cubes. What is the probability of rolling double threes?

$$\frac{1}{6} \cdot \frac{1}{6} = \frac{1}{36} \text{ or } \approx 0.027$$